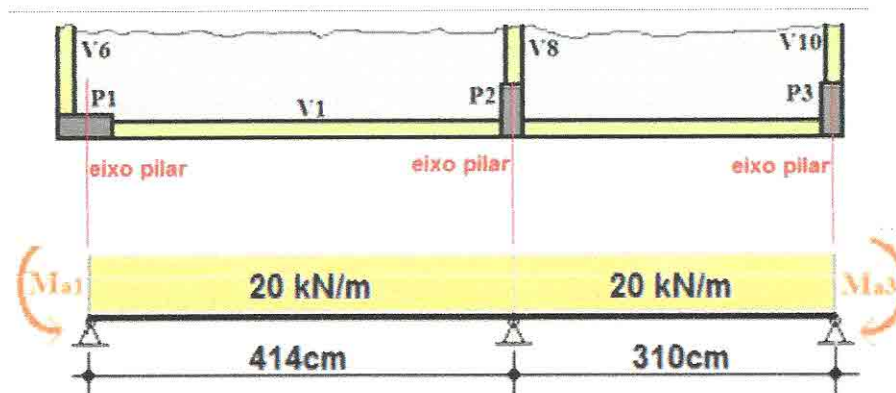


CONCRETO ARMADO I

Viga V1

i) Esquema estático:



ii) Momento de semi-engastamento Ma1:

$$\bullet I_{v1,a} = \frac{I_{v1}}{L_{v1}} = \frac{b \cdot h^3}{12 \cdot L_{v1}} = \frac{14 \cdot 40^3}{12 \cdot 414} = 180,35 \text{ cm}^3 \quad \bullet r_{i1} = r_{s1} = \frac{I_{p1}}{L_{p1}} = \frac{b \cdot h^3}{12 \cdot L_{p1}} = \frac{20 \cdot 40^3}{12 \cdot 300} = 355,56 \text{ cm}^3$$

$$\bullet M_{eng1} = \frac{p \cdot L_v^2}{12} = \frac{20 \cdot 4,14^2}{12} = 28,57 \text{ kN.m}$$

$$\bullet M_{a1} = M_{eng1} \cdot \frac{r_i + r_s}{r_i + r_s + r_v} = 28,57 \cdot \frac{355,56 + 355,56}{355,56 + 355,56 + 180,35} = 22,79 \text{ kN.m}$$

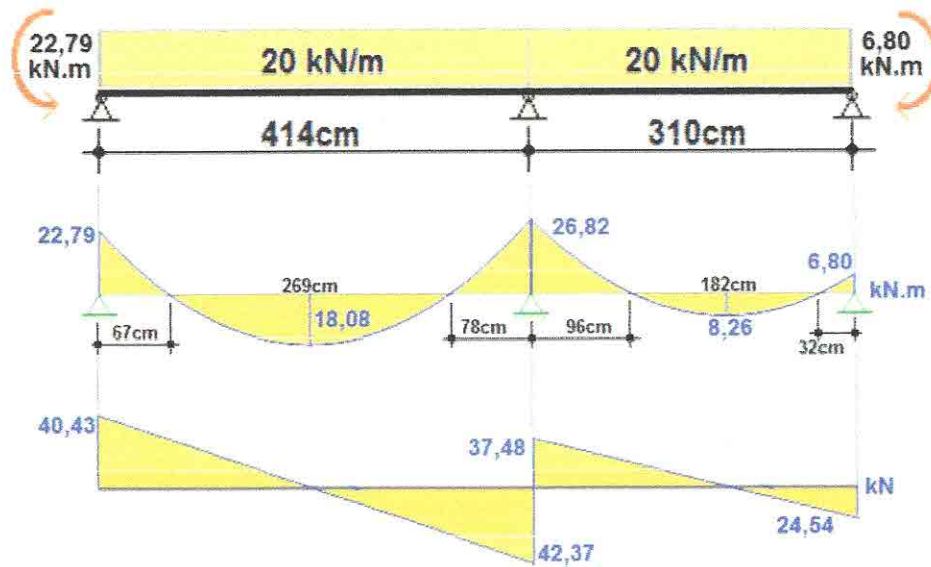
ii) Momento de semi-engastamento Ma3:

$$\bullet r_{v1,b} = \frac{I_v}{L_v} = \frac{b \cdot h^3}{12 \cdot L_v} = \frac{14 \cdot 40^3}{12 \cdot 310} = 240,86 \text{ cm}^3 \quad \bullet r_3 = r_{a3} = \frac{I_{p2}}{L_{p2}} = \frac{b \cdot h^3}{12 \cdot L_{p2}} = \frac{40 \cdot 20^3}{12 \cdot 300} = 88,89 \text{ cm}^3$$

$$\bullet M_{eng3} = \frac{p \cdot L_v^2}{12} = \frac{20 \cdot 3,10^2}{12} = 16,02 \text{ kN.m}$$

$$\bullet M_{a3} = M_{eng3} \cdot \frac{r_i + r_s}{r_i + r_s + r_v} = 16,02 \cdot \frac{88,89 + 88,89}{88,89 + 88,89 + 240,86} = 6,80 \text{ kN.m}$$

iii) Diagramas:



iv) Valor de A_s^+ : $M_k=18,08\text{kN.m}$

$$\bullet M_{dlim} = \mu_{lim} \cdot b \cdot d^2 \cdot f_{cd} = 0,32 \cdot 14 \cdot 35^2 \cdot \frac{2,5}{1,4} = 98,0 \text{ kN.m} > 1,4 \cdot 18,08 \rightarrow \text{Armadura simples}$$

$$\bullet y = d \cdot \left(1 - \sqrt{1 - \frac{M_d}{0,425 \cdot b \cdot d^2 \cdot f_{cd}}} \right) = 35 \cdot \left(1 - \sqrt{1 - \frac{1,4 \cdot 18,08 \cdot 100}{0,425 \cdot 14 \cdot 35^2 \cdot 2,5/1,4}} \right) = 3,59 \text{ cm}$$

$$\bullet A_s = \frac{0,85 \cdot f_{cd} \cdot b \cdot y}{f_{yd}} = \frac{0,85 \cdot 2,5/1,4 \cdot 14 \cdot 3,59}{50/1,15} = 1,75 \text{ cm}^2 \rightarrow A_s > A_{s \min} \rightarrow OK$$

$$\bullet A_{s \min} = \frac{\omega_{\min} \cdot A_c \cdot f_{cd}}{f_{yd}} = \frac{0,035 \cdot (14 \cdot 40) \cdot 2,5/1,4}{50/1,15} = 0,81 \text{ cm}^2$$

iv) Valor de A_s^+ : $M_k=8,26\text{kN.m}$

$$\bullet M_{dlim} = \mu_{lim} \cdot b \cdot d^2 \cdot f_{cd} = 0,32 \cdot 14 \cdot 35^2 \cdot \frac{2,5}{1,4} = 98,0\text{kN.m} > 1,4 \cdot 8,26 \rightarrow \text{Armadura simples}$$

$$\bullet y = d \cdot \left(1 - \sqrt{1 - \frac{M_d}{0,425 \cdot b \cdot d^2 \cdot f_{cd}}} \right) = 35 \cdot \left(1 - \sqrt{1 - \frac{1,4 \cdot 8,26 \cdot 100}{0,425 \cdot 14 \cdot 35^2 \cdot 2,5/1,4}} \right) = 1,59\text{cm}$$

$$\bullet A_s = \frac{0,85 \cdot f_{cd} \cdot b \cdot y}{f_{yd}} = \frac{0,85 \cdot 2,5/1,4 \cdot 14 \cdot 1,59}{50/1,15} = 0,78\text{cm}^2 \rightarrow A_s < A_{smin.}$$

$$\bullet A_{smin} = \frac{\omega_{min} \cdot A_c \cdot f_{cd}}{f_{yd}} = \frac{0,035 \cdot (14 \cdot 40) \cdot 2,5/1,4}{50/1,15} = 0,81\text{cm}^2 \quad A_s = A_{smin.} = 0,81\text{cm}^2$$

iv) Valor de A_s^- : $M_k=26,82\text{kN.m}$

$$\bullet M_{dlim} = \mu_{lim} \cdot b \cdot d^2 \cdot f_{cd} = 0,32 \cdot 14 \cdot 35^2 \cdot \frac{2,5}{1,4} = 98,0\text{kN.m} > 1,4 \cdot 26,82 \rightarrow \text{Armadura simples}$$

$$\bullet y = d \cdot \left(1 - \sqrt{1 - \frac{M_d}{0,425 \cdot b \cdot d^2 \cdot f_{cd}}} \right) = 35 \cdot \left(1 - \sqrt{1 - \frac{1,4 \cdot 26,82 \cdot 100}{0,425 \cdot 14 \cdot 35^2 \cdot 2,5/1,4}} \right) = 5,48\text{cm}$$

$$\bullet A_s = \frac{0,85 \cdot f_{cd} \cdot b \cdot y}{f_{yd}} = \frac{0,85 \cdot 2,5/1,4 \cdot 14 \cdot 5,48}{50/1,15} = 2,68\text{cm}^2 \rightarrow A_s > A_{smin.} \rightarrow OK$$

$$\bullet A_{smin} = \frac{\omega_{min} \cdot A_c \cdot f_{cd}}{f_{yd}} = \frac{0,035 \cdot (14 \cdot 40) \cdot 2,5/1,4}{50/1,15} = 0,81\text{cm}^2$$

iv) Valor de A_s^- : $M_k=22,79\text{kN.m}$

$$\bullet M_{dlim} = \mu_{lim} \cdot b \cdot d^2 \cdot f_{cd} = 0,32 \cdot 14 \cdot 35^2 \cdot \frac{2,5}{1,4} = 98,0\text{kN.m} > 1,4 \cdot 22,79 \rightarrow \text{Armadura simples}$$

$$\bullet y = d \cdot \left(1 - \sqrt{1 - \frac{M_d}{0,425 \cdot b \cdot d^2 \cdot f_{cd}}} \right) = 35 \cdot \left(1 - \sqrt{1 - \frac{1,4 \cdot 22,79 \cdot 100}{0,425 \cdot 14 \cdot 35^2 \cdot 2,5/1,4}} \right) = 4,59\text{cm}$$

$$\bullet A_s = \frac{0,85 \cdot f_{cd} \cdot b \cdot y}{f_{yd}} = \frac{0,85 \cdot 2,5/1,4 \cdot 14 \cdot 4,59}{50/1,15} = 2,24\text{cm}^2 \rightarrow A_s > A_{smin.} \rightarrow OK$$

$$\bullet A_{smin} = \frac{\omega_{min} \cdot A_c \cdot f_{cd}}{f_{yd}} = \frac{0,035 \cdot (14 \cdot 40) \cdot 2,5/1,4}{50/1,15} = 0,81\text{cm}^2$$

v) Armadura de projeto e verificações:

- $As^- = 0,81\text{cm}^2 \rightarrow A_{proj} = 2\phi 8,0 (1,00\text{cm}^2)$

- $e_h > \begin{cases} - 20\text{mm} = 2,0\text{cm} \\ - \text{diâmetro da barra, feixe, ou luva} = 0,8\text{cm} \\ - 1,2 \cdot d_{max} = 1,2 \cdot 19\text{mm} = 2,28\text{cm} \\ - \text{vibrador} = 4\text{cm (arm. negativa)} \end{cases} \rightarrow e_h \geq 4,0\text{cm}$

- $e_h = 14 - 2 \cdot \text{Cobr} - 2 \cdot \phi_t - 2 \cdot 1,25 = 4,5\text{cm} \Rightarrow 4,5\text{cm} > 4,0\text{cm} \rightarrow OK$

- $d'_r = \text{Cobr} + \phi_t + \frac{0,8}{2} = 3,90\text{cm} \rightarrow 3,9\text{cm} < 5,0\text{cm} \rightarrow OK$

- $a = 0 \rightarrow 0 < 5\% \cdot h = 2,0\text{cm} \rightarrow OK \text{ (Rcc} \leftrightarrow \text{CG)}$

v) Armadura de projeto e verificações:

- $As^- = 2,68\text{cm}^2 \rightarrow A_{proj} = \begin{cases} - 2\phi 16,0 (4,0\text{cm}^2) \\ - 4\phi 10,0 (3,2\text{cm}^2) \end{cases} \rightarrow A_{proj} = 2\phi 12,5$

- $e_h > \begin{cases} - 20\text{mm} = 2,0\text{cm} \\ - \text{diâmetro da barra, feixe, ou luva} = 1,25\text{cm} \\ - 1,2 \cdot d_{max} = 1,2 \cdot 19\text{mm} = 2,28\text{cm} \\ - \text{vibrador} = 4\text{cm (arm. negativa)} \end{cases} \rightarrow e_h \geq 4,0\text{cm}$

- $e_h = 14 - 2 \cdot \text{Cobr} - 2 \cdot \phi_t - 2 \cdot 1,25 = 4,5\text{cm} \Rightarrow 4,5\text{cm} > 4,0\text{cm} \rightarrow OK$

- $d'_r = \text{Cobr} + \phi_t + \frac{1,25}{2} = 4,13\text{cm} \rightarrow 4,13\text{cm} < 5,0\text{cm} \rightarrow OK$

- $a = 0 \rightarrow 0 < 5\% \cdot h = 2,0\text{cm} \rightarrow OK \text{ (Rcc} \leftrightarrow \text{CG)}$

v) Armadura de projeto e verificações:

$$\bullet A_s^- = 2,24 \text{ cm}^2 \rightarrow A_{\text{proj}} = \begin{cases} - 2\phi 12,5 (2,5 \text{ cm}^2) \\ - 4\phi 10,0 (3,2 \text{ cm}^2) \end{cases} \rightarrow A_{\text{proj}} = 2\phi 12,5$$

$$\bullet e_h > \begin{cases} - 20 \text{ mm} = 2,0 \text{ cm} \\ - \text{diâmetro da barra, feixe, ou luva} = 1,25 \text{ cm} \\ - 1,2 \cdot d_{\text{max}} = 1,2 \cdot 19 \text{ mm} = 2,28 \text{ cm} \\ - \text{vibrador} = 4 \text{ cm (arm. negativa)} \end{cases} \rightarrow e_h \geq 4,0 \text{ cm}$$

$$\bullet e_h = 14 - 2 \cdot \text{Cobr} - 2 \cdot \phi_t - 2 \cdot 1,25 = 4,5 \text{ cm} \Rightarrow 4,5 \text{ cm} > 4,0 \text{ cm} \rightarrow \text{OK}$$

$$\bullet d'_r = \text{Cobr} + \phi_t + \frac{1,25}{2} = 4,13 \text{ cm} \rightarrow 4,13 \text{ cm} < 5,0 \text{ cm} \rightarrow \text{OK}$$

$$\bullet a = 0 \rightarrow 0 < 5\% \cdot h = 2,0 \text{ cm} \rightarrow \text{OK} \quad (R_{sc} \leftrightarrow CG)$$

vi) Armadura apoios externos:

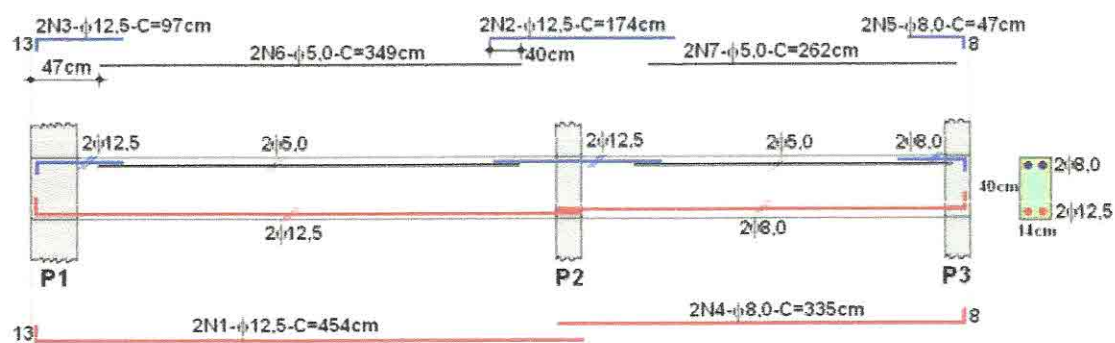
$$\bullet A_{s, \text{esquerdo}} > \begin{cases} - 2\phi \\ - |M_{\text{apoio}}| > \frac{M_{\text{vão}}}{2} \rightarrow \frac{A_{s, \text{vão}}}{4} \rightarrow \frac{2,24}{4} = 0,56 \text{ cm}^2 \\ - \frac{\alpha_l V_d}{d \cdot f_{yd}} \rightarrow \text{Não (momento} \neq 0) \end{cases} \Rightarrow A_{\text{apoio}} = 2\phi 12,5$$

(Em P1)

$$\bullet A_{s, \text{direito}} > \begin{cases} - 2\phi \\ - |M_{\text{apoio}}| > \frac{M_{\text{vão}}}{2} \rightarrow \frac{A_{s, \text{vão}}}{4} \rightarrow \frac{0,81}{4} = 0,20 \text{ cm}^2 \\ - \frac{\alpha_l V_d}{d \cdot f_{yd}} \rightarrow \text{Não (momento} \neq 0) \end{cases} \Rightarrow A_{\text{apoio}} = 2\phi 8,0$$

(Em P3)

vii) Detalhamento:



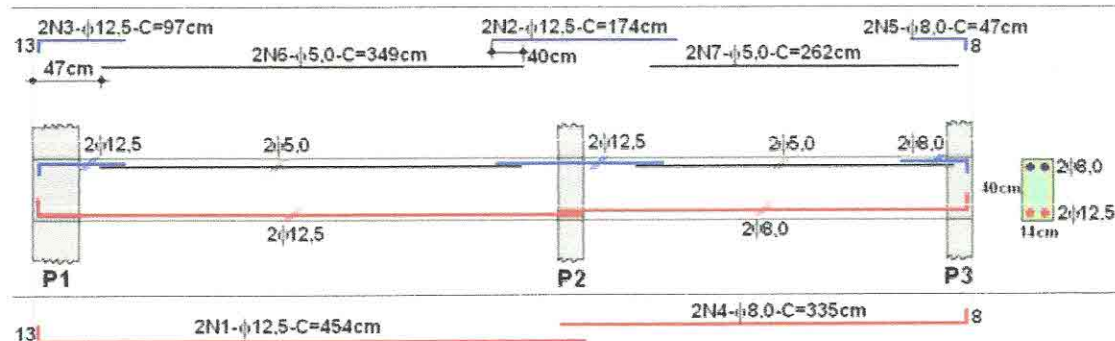
$$\bullet N_1 = 414 + \frac{40}{2} - 3 + 13 + \frac{20}{2} = 454 \text{ cm}$$

$$\bullet N_3 = 67 + \frac{40}{2} - 3 + 13 = 97 \text{ cm}$$

$$\bullet N_2 = 78 + 96 = 174 \text{ cm}$$

$$\bullet N_4 = 310 + \frac{20}{2} - 3 + 8 + \frac{20}{2} = 335 \text{ cm}$$

vii) Detalhamento:



$$\bullet N_5 = 32 + \frac{20}{2} - 3 + 8 = 47 \text{ cm}$$

$$\bullet N_7 = 182 + 2.40 = 262 \text{ cm}$$

$$\bullet N_6 = 289 + 2.40 = 349 \text{ cm}$$

iv) Valor de As^- : $M_k=6,80\text{kN.m}$

$$\bullet M_{\text{lim}} = \mu_{\text{lim}} \cdot b \cdot d^2 \cdot f_{cd} = 0,32 \cdot 14 \cdot 35^2 \cdot \frac{2,5}{1,4} = 98,0\text{kN.m} > 1,4 \cdot 6,80 \rightarrow \text{Armadura simples}$$

$$\bullet y = d \cdot \left(1 - \sqrt{1 - \frac{M_d}{0,425 \cdot b \cdot d^2 \cdot f_{cd}}} \right) = 35 \cdot \left(1 - \sqrt{1 - \frac{1,4 \cdot 6,80 \cdot 100}{0,425 \cdot 14 \cdot 35^2 \cdot 2,5/1,4}} \right) = 1,30\text{cm}$$

$$\bullet As = \frac{0,85 \cdot f_{cd} \cdot b \cdot y}{f_{yd}} = \frac{0,85 \cdot 2,5/1,4 \cdot 14 \cdot 1,30}{50/1,15} = 0,64\text{cm}^2 \rightarrow As < As_{\text{min.}}$$

$$\bullet As_{\text{min}} = \frac{\omega_{\text{min}} \cdot A_c \cdot f_{cd}}{f_{yd}} = \frac{0,035 \cdot (14 \cdot 40) \cdot 2,5/1,4}{50/1,15} = 0,81\text{cm}^2 \quad \downarrow \quad As = As_{\text{min.}} = 0,81\text{cm}^2$$

v) Armadura de projeto e verificações:

$$\bullet As^+ = 1,75\text{cm}^2 \rightarrow A_{\text{proj}} = 2\phi 12,5 (2,50\text{cm}^2)$$

$$\bullet e_h > \begin{cases} - 20\text{mm} = 2,0\text{cm} \\ - \text{diâmetro da barra, feixe, ou luva} = 1,25\text{cm} \\ - 1,2 \cdot d_{\text{max}} = 1,2 \cdot 19\text{mm} = 2,28\text{cm} \end{cases} \rightarrow e_h \geq 2,28\text{cm}$$

$$\bullet e_h = 14 - 2 \cdot \text{Cobr} - 2 \cdot \phi_t - 2 \cdot 1,25 = 4,5\text{cm} \Rightarrow 4,5\text{cm} > 2,28\text{cm} \rightarrow \text{OK}$$

$$\bullet d'_r = \text{Cobr} + \phi_t + \frac{1,25}{2} = 4,13\text{cm} \rightarrow 4,13\text{cm} < 5,0\text{cm} \rightarrow \text{OK}$$

$$\bullet a = 0 \rightarrow 0 < 5\% \cdot h = 2,0\text{cm} \rightarrow \text{OK} \quad (R_{cc} \leftrightarrow CG)$$

v) Armadura de projeto e verificações:

$$\bullet As^+ \text{ e } As^- = 0,81\text{cm}^2 \rightarrow A_{\text{proj}} = 2\phi 8,0 (1,00\text{cm}^2)$$

$$\bullet e_h > \begin{cases} - 20\text{mm} = 2,0\text{cm} \\ - \text{diâmetro da barra, feixe, ou luva} = 0,8\text{cm} \\ - 1,2 \cdot d_{\text{max}} = 1,2 \cdot 19\text{mm} = 2,28\text{cm} \\ - \text{vibrador} = 4\text{cm (arm. negativa)} \end{cases} \rightarrow e_h \geq 4,0\text{cm}$$

$$\bullet e_h = 14 - 2 \cdot \text{Cobr} - 2 \cdot \phi_t - 2 \cdot 1,25 = 4,5\text{cm} \Rightarrow 4,5\text{cm} > 4,0\text{cm} \rightarrow \text{OK}$$

$$\bullet d'_r = \text{Cobr} + \phi_t + \frac{0,8}{2} = 3,90\text{cm} \rightarrow 3,9\text{cm} < 5,0\text{cm} \rightarrow \text{OK}$$

$$\bullet a = 0 \rightarrow 0 < 5\% \cdot h = 2,0\text{cm} \rightarrow \text{OK} \quad (R_{cc} \leftrightarrow CG)$$